

The Role of Design Complexity in Technology Improvement

James McNerney
J. Doyne Farmer
Sid Redner
Jessika E. Trancik

SFI WORKING PAPER: 2009-07-023

SFI Working Papers contain accounts of scientific work of the author(s) and do not necessarily represent the views of the Santa Fe Institute. We accept papers intended for publication in peer-reviewed journals or proceedings volumes, but not papers that have already appeared in print. Except for papers by our external faculty, papers must be based on work done at SFI, inspired by an invited visit to or collaboration at SFI, or funded by an SFI grant.

©NOTICE: This working paper is included by permission of the contributing author(s) as a means to ensure timely distribution of the scholarly and technical work on a non-commercial basis. Copyright and all rights therein are maintained by the author(s). It is understood that all persons copying this information will adhere to the terms and constraints invoked by each author's copyright. These works may be reposted only with the explicit permission of the copyright holder.

www.santafe.edu



SANTA FE INSTITUTE

The Role of Design Complexity in Technology Improvement

James McNerney ^{* †}, J. Doyne Farmer ^{* ‡}, Sid Redner ^{* † §}, and Jessika E Trancik ^{* ¶}

^{*}Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, NM 87501, USA, [†]Department of Physics, Boston University, Boston, MA 02215, USA, [‡]LUISS Guido Carli, Viale Pola 12, 00198, Roma, Italy, [§]Center for Polymer Studies, Boston University, Boston, MA 02215, USA, and [¶]Earth Institute, Columbia University, New York, NY 10027

Submitted to Proceedings of the National Academy of Sciences of the United States of America

We study a simple model for the evolution of the cost (or more generally the performance) of a technology or production process. The technology can be decomposed into n components, each of which interacts with a cluster of $d - 1$ other, dependent components. Innovation occurs through a series of trial-and-error events, each of which consists of randomly changing the cost of each component in a cluster, and accepting the changes only if the total cost of the entire cluster is lowered. We show that the relationship between the cost of the whole technology and the number of innovation attempts is asymptotically a power law, matching the functional form often observed for empirical data. The exponent α of the power law depends on the intrinsic difficulty of finding better components, and on what we term the design complexity: The more complex the design, the slower the rate of improvement. Letting d as defined above be the connectivity, in the special case in which the connectivity is constant, the design complexity is simply the connectivity. When the connectivity varies, bottlenecks can arise in which a few components limit progress. In this case the design complexity is more complicated, depending on the details of the design. The number of bottlenecks also determines whether progress is steady, or whether there are periods of stasis punctuated by occasional large changes. Our model connects the engineering properties of a design to historical studies of technology improvement.

experience curve | learning curve | progress function | performance curve | design structure matrix | evolution of technology

The relation between a technology's cost c and the cumulative amount produced y is often empirically observed to be a power law of the form

$$c(y) \propto y^{-\alpha}, \quad [1]$$

where the exponent α characterizes the rate of improvement. This rate is commonly termed the *progress ratio* $2^{-\alpha}$, which is the factor by which costs decrease with each doubling of cumulative production. A typical reported value [9] is 0.8 (corresponding to $\alpha \approx .32$), which implies that the cost of the 200th item is 80% that of the 100th item. Power laws have been observed, or at least assumed to hold, for a wide variety of technologies [2, 18, 9], although other functional forms have also been suggested and in some cases provide plausible fits to the data¹. We give examples of historical performance curves for several different technologies in Figure 1.

The relationship between cost and cumulative production goes under several different names, including the “experience curve”, the “learning curve” or the “progress function”. The terms are used interchangeably by some, while others assign distinct meanings [9, 29]. We use the general term *performance curve* to denote a plot of any performance measure (such as cost) against any experience measure (such as cumulative production), regardless of the context. Performance curve studies first appeared in the 19th century [10, 6], but their application to manufacturing and technology originates from the 1936 study by Wright on aircraft production costs [31]. The large literature on this subject spans engineering [23], economics [3, 29], management science [9], and public policy [30]. Performance curves have been constructed for individuals, production processes, firms, and industries [9].

The power law assumption has been used by firm managers [12] and government policy makers [30] to forecast how costs will drop with cumulative production. However, the po-

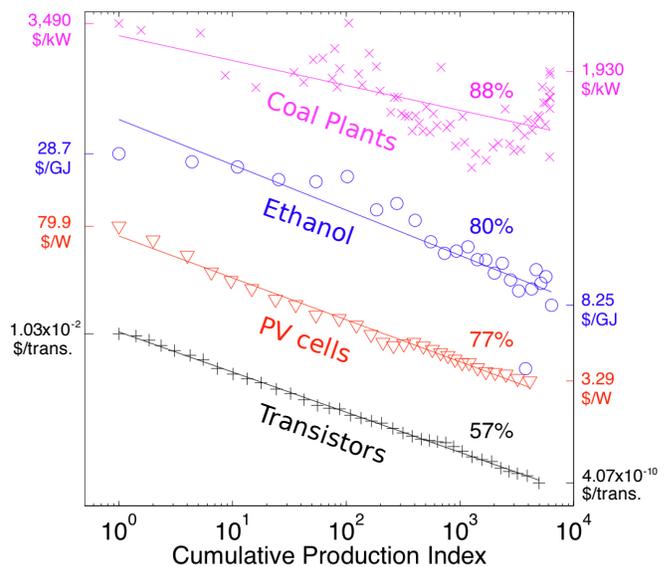


Fig. 1: Four empirical performance curves. Each curve was rescaled and shifted to aid comparison with a power law. The x - and y - coordinates of each series i were transformed via $\log x \rightarrow a_i + b_i \log x$, $\log y \rightarrow c_i + d_i \log y$. The constants a_i , b_i , c_i , and d_i were chosen to yield series with approximately the same slope and range, and are given in the Supporting Information. Tick marks and labels on the left vertical axis show the first price (in real 2000 dollars) of the corresponding time series, and those of the right vertical axis show the last price. Lines are least-squares fits to a power law. Percentages are the progress ratios of the fitted power laws. Source: coal plants [14], ethanol [1], photovoltaic cells [21, 28, 17], transistors [19].

Reserved for Publication Footnotes

¹ Koh and Magee [15, 16] claim an exponential function of time (Moore's law) predicts the performance of several different technologies. Goddard [11] claims costs follow a power law in production rate rather than cumulative production. Multivariate forms involving combinations of production rate, cumulative production, or time have been examined by Sinclair et al. [26] and Nordhaus [22].

tential for exploiting performance curves has so far not been fully realized, in part because there is no theory explaining the observed empirical relationships. Why do performance curves tend to look like power laws, as opposed to some other functional form? What factors determine the exponent α , which governs the long-term rate of improvement? Why are some performance curves steady and others erratic? By suggesting answers to these questions, the theory we develop here can potentially be used to guide investment policy for technological change.

A good example of the possible usefulness of such a theory is climate change mitigation. Good forecasts of future costs of low-carbon energy technologies could help guide research and development funding and climate policy. Our theory suggests that based on the design of a technology we might be able to better forecast its rate of improvement, and therefore make better investments and better estimates of the cost of achieving low-carbon energy generation.

There have been several previous attempts to construct theories to explain the functional form of performance curves [20, 4, 13]. Muth constructed a model of a single-component technology in which innovation happens by proposing new designs at random. Using extreme value theory he derived conditions under which the rate of improvement is a power law. An extension to multiple components, called the *production recipe model*, was proposed by Auerswald et al. [4]. In their model each component interacts with other components, and if a given component is replaced, it affects the cost of the components with which it interacts. They simulated their model and found that under some circumstances the performance curves appeared to be power laws.

We simplify the production recipe model in order to make it more tractable. This simplification allows us to derive the emergence of a power law, and in particular, to derive its exponent α . We obtain the result that the asymptotic rate of improvement is independent of the total number of components n . Instead we find that $\alpha = 1/(\gamma d^*)$, where γ measures the intrinsic difficulty of finding better components and d^* is what we call the *design complexity*. When the connectivity of the components is constant, the design complexity is equal to the connectivity, but when connectivity varies, it can also depend on the detailed properties of the design. We also show that when costs are spread uniformly across a large number of components, the whole technology undergoes steady improvement. In contrast, when costs are dominated by a few components, it undergoes erratic improvement. Our theory thus potentially gives insight into how to design a technology so that it will improve more rapidly and more steadily.

The Model

The production design consists of n components, which can be thought of as the parts of a technology or the steps in an industrial process.² Each component i has a cost c_i . The total cost c of the design is the sum of the component costs: $c = c_1 + c_2 + \dots + c_n$. A component's cost changes as new implementations for the component are found. For example, a component representing the step "move a box across a room" may initially be implemented by a forklift, which could later be replaced by a conveyor belt. Cost reductions occur through repeated changes to one or more components.

Components are not isolated from one another, but rather interact as parts of the overall design. Thus changing one component not only affects its cost, but also the costs of other *dependent* components. Components may be viewed as nodes in a directed network, with links from each component to those that depend on it. The relationship between the nodes and

links can alternately be characterized by an adjacency matrix. In systems engineering and management science this matrix is known as the *design structure matrix* or DSM [27, 25, 5]. A DSM is an $n \times n$ matrix with an entry in row i and column j if a change in component j , the modifying component, affects component i , the dependent component (Fig. 2). The matrix is usually binary [8, 24]; however, weighted interactions have also been considered [7]. DSMs have been found to be useful in understanding and improving complex manufacturing and technology development processes.

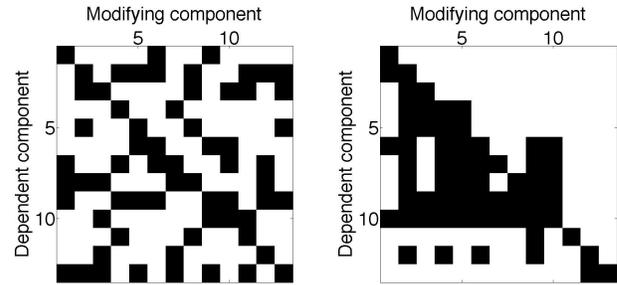


Fig. 2: Example dependency structure matrices (DSMs) with $n = 13$ components. Black squares represent links. The DSM on the left was randomly generated to have fixed out-degree for each component. The DSM on the right represents the design of an automobile brake system [24]. All diagonal elements are present because a component always affects its own cost.

We begin by considering the simplest case of *fixed out-degree*, or equivalently constant *connectivity*, in which each component affects exactly d components: itself and $d - 1$ others. The dependencies between components are chosen at random with equal probability. Cost reductions are realized through the following series of innovation attempts:

1. Pick a random component i .
2. Use the DSM to identify the set of dependent components $\mathcal{A}_i = \{j\}$ whose costs depend on i .
3. Determine a new cost c'_j for each component $j \in \mathcal{A}_i$ from a specified probability distribution f .
4. If the sum of the new costs, $C'_i = \sum_{j \in \mathcal{A}_i} c'_j$, is less than the current sum, C_i , then each c_j is changed to c'_j . Otherwise, the new cost set is rejected.

The costs are defined on $[0, 1]$. We assume a probability density function that for small values of c_i has the form $f(c_i) \propto c_i^{\gamma-1}$, i.e. the cumulative distribution $F(c_i) = \int_0^{c_i} f(c)dc \propto c_i^\gamma$. The exponent γ specifies the difficulty of reducing costs of individual components, with higher γ corresponding to higher difficulty. This functional form is fairly general in that it covers any distribution with a valid power-series expansion at $c = 0$.

Independent Components

Let us first consider the process with a single component, as originally studied by Muth [20]. The generalization to n inde-

² The original production recipe model contained 6 parameters. The following simplifications were made to produce the model in this paper: Length of production run $T \rightarrow \infty$. Output-per-attempted-recipe-change $\bar{B} \rightarrow 1$. Available implementations per component $s \rightarrow \infty$. Search distance $\delta \rightarrow 1$.

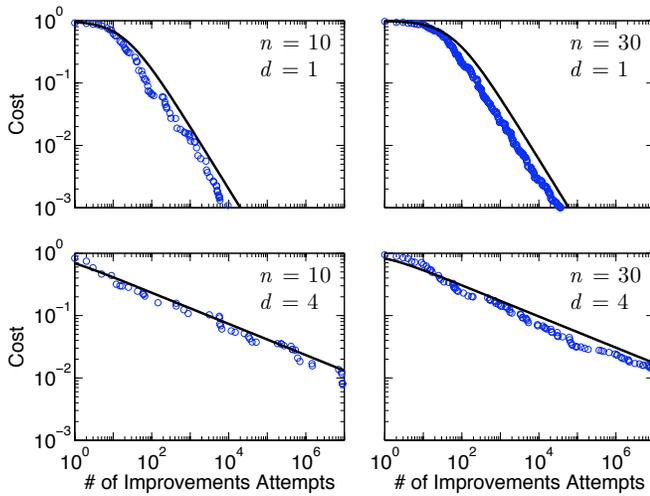


Fig. 4: Simulations of single realizations of the model for various numbers of components n and design complexity $d^* = d$, using DSMs with constant d . The plots are for $n = 10, 30$ and $d = 1, 4$. The solid curves represent Eq. [5].

pendent components is trivial, and only affects the constant of proportionality. Letting t represent the number of innovation steps, the cost at time t is equivalent to the minimum of t independent, identically-distributed random variables. In the Supporting Information we show that the exact solution when $\gamma = 1$ is

$$c(t) = \frac{1}{1+t}. \quad [2]$$

We now present an intuitive derivation that gives the right scaling but underestimates the amplitude. At each innovation attempt a new cost c' is drawn uniformly from $[0, 1]$, and a successful reduction occurs if c' is less than the current cost c . Since the distribution of new costs is uniform on $[0, 1]$ the probability $\text{Prob}(c' < c)$ that c' represents a reduction simply equals c . When a reduction does occur, the average value of c' equals $c/2$. In continuous time the rate of change of the average component cost is

$$\frac{dc}{dt} \sim -\left(\frac{c}{2}\right) \times \text{Prob}(c' < c) = -\frac{1}{2}c^2. \quad [3]$$

The solution to Eq. [3] gives the correct scaling of $c(t) \sim 1/t$ as $t \rightarrow \infty$. One way to view this result is that cost reductions are proportional to the cost itself, leading to an exponential decrease in cost with each reduction event; however, each reduction takes exponentially longer to achieve as the cost decreases. The competition between these two exponentials yields a power law. Muth's result is an application of extreme value theory, in which the mean value of the minimum of m independent and identically distributed random variables evolves as a power law in m when the variables are drawn from a distribution with a power-series expansion around zero.

Interacting Components, Fixed Out-Degree

Now consider an n -component process with fixed out-degree, where each component affects exactly $d - 1$ other, dependent components. Following steps similar to those that led to Eq. [3], let $c(t)$ denote the current total cost of all components. The average change in c due to the next improvement

is given by summing over all changes that result in a new cost $c' < c$, and multiplying the changes by their respective probabilities:

$$\langle \Delta c \rangle \approx - \int_0^c p(c')(c - c') dc'.$$

This integral is performed in the Supporting Information. The average change per timestep is

$$\frac{dc}{dt} \approx -Kc^{\gamma d+1}, \quad [4]$$

where

$$K = \frac{1}{n} d^{\gamma d+1} \gamma^d \prod_{j=0}^{d-1} B(\gamma, j\gamma + 2),$$

and $B(p, q)$ is the Beta function. The solution to Eq. [4] is

$$c(t) = c(0) \left(\frac{t}{t_0} + 1 \right)^{-\frac{1}{\gamma d}}, \quad [5]$$

with $t_0 = [Kc(0)^{\gamma d} \gamma d]^{-1}$.

We compare our prediction in Eq. [5] to simulations in Fig. . Initially each component cost c_i is set to $1/n$, so that the total initial cost $c(0) = 1$, and we arbitrarily choose $\gamma = 1$. Our theory correctly predicts the asymptotic power law scaling of the simulated performance curves. Furthermore our theory predicts an initial downward concavity that lasts for a time t_0 ; this prediction is accurate for small d (but for large d it underestimates the concavity). As given by Eq. [5], increasing the number of components n extends the duration of the initial concavity.

The above asymptotic solution for $c(t)$ is consistently somewhat larger than the average value in the simulation. This discrepancy stems from the approximations involved in deriving Eq. [5]. In the Supporting Information the average cost is derived by other methods that compute the distribution. These calculations yield the correct amplitude but only apply in the limit $t \rightarrow \infty$.

The salient result of this section is that the exponent $\alpha = 1/(\gamma d)$ of the performance curve is directly and simply related to the out-degree d , which can be viewed as a measure of the complexity of the design, and γ , which characterizes the difficulty of improving individual components in the limit as the cost goes to zero. If $\gamma d = 1$ then $\alpha = 1$ and the progress ratio $2^{-1/(\gamma d)}$ is 50%. If $\gamma d = 3$ then $\alpha = 1/3$ and the progress ratio is approximately 80%, a common value observed in empirical performance curves.

Interacting Components, Variable Out-Degree

When the out-degree of each component is variable the situation is more interesting and more realistic because components may differ in their rate of improvement [24]. Slowly improving components can create bottlenecks that hinder the overall rate of improvement. To understand why such bottlenecks occur it is important to realize that the rate of improvement of a given component depends on all the clusters A_j of which it is a member. (Recall that A_j is the set of components affected by j .) As illustrated in Figure 3, there are two ways to reduce the cost of component i :

1. Pick i and improve cluster A_i .
2. Pick another modifying component j that affects i and improve cluster A_j .

As we shall now show, the limiting rate for the improvement of a given component i is determined not only by the out-degree of the component itself, but also by the properties of the clusters A_j of the modifying components that affect it.

First consider process (1) in which component i is picked, corresponding to the dotted ellipse in Figure 3. Let $C_i = \sum_{k \in \mathcal{A}_i} c_k$ be the sum of the costs of the d_i dependent components in \mathcal{A}_i . Since d_i new costs are drawn independently at each time step the generation of new costs is equivalent to picking a point with uniform probability in a d_i -dimensional hypercube. The combinations of component costs that reduce the total cost lie within the simplex defined by $\sum_{k \in \mathcal{A}_i} c'_k < C_i$, where c'_k are the new costs. The probability of reducing the cost is therefore the ratio of the simplex volume to the hypercube volume,

$$p_i = \frac{(C_i^{d_i}/d_i!)}{(1/n)^{d_i}} = \frac{(nC_i)^{d_i}}{d_i!}, \quad [6]$$

which is a decreasing function of d_i . Thus a component with a higher out-degree (greater connectivity) is less likely to be improved when chosen. (This is essentially the reason why α decreases with d when the out-degree is fixed.)

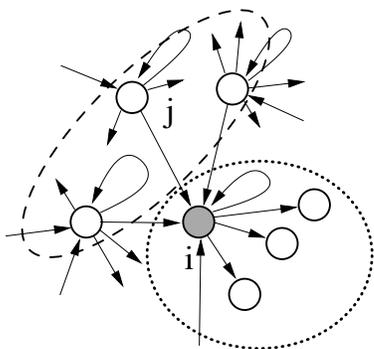


Fig. 3: A component i (shaded circle), together with the dependent components \mathcal{A}_i that are affected by i (dotted ellipse) and the modifying components that affect i (dashed ellipse). The arrow from j to i indicates that a change in cost of component j affects the cost of i .

Let us now consider case (2) in which component i improves when another modifying component j that affects it is chosen (lying inside the dashed ellipse in Fig. 3). Any component j whose cluster contains i can cause an improvement. Let d_j^i be the out-degree of the modifying components j that affect i . Then the overall rate at which i improves is determined by $d_i^{\min} = \min_j \{d_j^i\}$, i.e. by the component j most likely to cause an improvement in i . The overall improvement rate for the whole technology is then determined by the slowest improving component i . Thus the design complexity is more generally given by

$$d^* = \max_i \{d_i^{\min}\}. \quad [7]$$

Note that in the case of constant out-degree d this reduces to $d^* = d$. In every case we have studied $\alpha = 1/(d^* \gamma)$ correctly predicts the mean rate of improvement when t is sufficiently large (see Fig. 5).

Fluctuations

The analysis we have given provides insight not only into the mean behavior, but also into the fluctuations about the mean, which can behave quite differently depending on the properties of the DSM. In Fig. 5 we plot two individual trajectories of cost vs. time for each of three different DSMs. The trajectories fluctuate in every case, but the amplitude of fluctuations is highly variable. In the left panel the amplitude of the fluctuations remains relatively small and is roughly constant in time when plotted on double logarithmic scale (indicating that the amplitude of the fluctuations is always proportional to the mean). For the middle and right panels, in contrast, the individual trajectories show a random staircase behavior, and the amplitude of the fluctuations continues to grow for a longer time.

This behavior can be explained in terms of the improvement rates d_i^{\min} for each component. The maximum value of d_i^{\min} determines the slowest-improving components. In the left panel the maximum value of $d_i^{\min} = 2$. This value is repeated four times. After a long time these four components dominate the overall cost. However, since they have the same values of d_i^{\min} their contributions remain comparable, and the total cost is averaged over all four of them, keeping the fluctuations relatively small. (See the lower panels of Fig. 5.)

In contrast, in the middle panel we illustrate a DSM where the slowest-improving component (number 7) has $d_7^{\min} = 4$ and the next slowest-improving component (number 6) has $d_6^{\min} = 2$. With the passage of time component 7 comes to dominate the cost. This component is slow to improve because it is rarely chosen for improvement. But in the rare cases that component 7 is chosen the improvements can be dramatic, generating large downward steps in its trajectory. The right case illustrates an intermediate situation where two components are dominant.

Another striking feature of the distribution of trajectories is the difference between the top and bottom envelopes of the plot of the distribution vs. time. In every case the top envelope follows a straight line throughout most of the time range. The behavior of the bottom envelope is more complicated; in many cases, such as the left panel of Fig. 5, it also follows a straight line, but in others, for example the middle panel, the bottom envelope changes slope over a large time range. A more precise statement can be made by following the contour corresponding to a given quantile through time. All quantiles eventually approach a line with slope $1/d^*$. However, the upper quantiles converge to this line quickly, whereas in some cases the lower quantiles do so much later. This slower convergence stems from the difference in improvement rates of different components. Whenever there is a dramatic improvement in the slowest-improving component (or components), there is a period where the next slowest-improving component (or components) becomes important. During this time the lower d_i^{\min} value of the second component temporarily influences the rate of improvement. After a long time the slowest-improving component becomes more and more dominant, large updates become progressively more rare, and the slope becomes constant.

The model therefore suggests that properties of the design determine whether a technology's improvement will be steady or erratic. Homogeneous designs (with constant out-degree) are more likely to show an inexorable trend of steady improvement. Heterogeneous designs (with larger variability in out-degree) are more likely to improve in fits and starts. High variability among individual trajectories can be interpreted as indicating that historical contingency plays an important role. By this we mean that the particular choice of random numbers, rather than the overall trend, dominates the behavior.

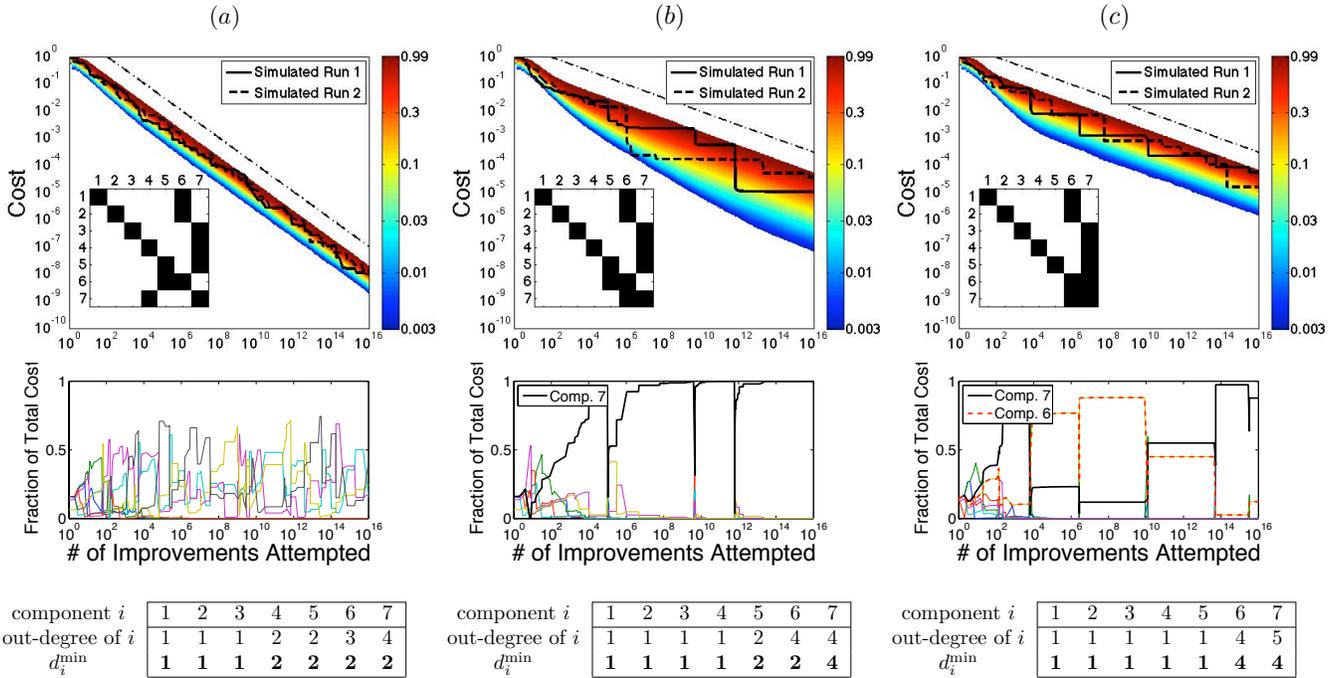


Fig. 5: Evolution of the distribution of costs. Each figure in the top row shows a simulated distribution of costs as a function of time using the design structure matrix (DSM) in the lower left corner of each plot. The upper dash-dot lines provides a reference with the predicted slope $\alpha = 1/(\gamma d^*)$, with $\gamma = 1$; from left-to-right the slopes are $-1/2$, $-1/4$, and $-1/4$. The data for each DSM are the result of 50,000 realizations, corresponding to different random number seeds. The distributions are color coded to correspond to constant quantiles, i.e. the fraction of costs less than a given value at a given time. The solid and dashed black curves inside the colored regions represent two sample trajectories of the total cost as a function of time. The DSMs are constructed so that in each case component 1 has the lowest out-degree and component 7 has the highest out-degree. Below each distribution we plot the fraction of the total cost contributed by each of the 7 components at any given time (corresponding to the first simulation run). The components in Figs. (b) and (c) with the biggest contribution to the cost in the limit $t \rightarrow \infty$ are highlighted. The box at the bottom gives the value of d_i^{\min} for each component of the design.

In this case progress appears to come about through a series of punctuated equilibria.

To summarize, in this section we have shown that the asymptotic magnitude of the fluctuations is determined by the number of critical bottlenecks, defined as the number of components that have the maximum value of d_i^{\min} . In the constant out-degree case all of the components are equivalent, and this number is just n . In the variable out-degree case, however, this number depends on the details of the DSM, which influence d_i^{\min} . The fluctuations decrease as the number of worst bottlenecks increases.

Testing the Model Predictions

Our model makes the testable prediction that the rate of improvement of a technology depends on the design complexity, which can be determined from a design structure matrix. The use of DSMs to analyze designs is widespread in the systems engineering and management science literature. Thus, one could potentially examine the DSMs of different technologies, compute their corresponding design complexities, and compare to the value of α based on the technology's history³.

This test is complicated by the fact that α also depends on γ , which describes the inherent difficulty of improving individual components, which in turn depends on the inherent difficulty of the innovation problem as well as the collective effectiveness of inventors in generating improvements. The exponent γ is problematic to measure independently. Nonetheless, one could examine a collection of different technologies

and either assume that γ is constant or that the variations in γ average out. Subject to these caveats, the model then predicts that the design complexity of the DSM should be inversely proportional to the estimated α of the historical trajectory. A byproduct of such a study is that it would yield an estimate of γ in different technologies.

To compare the model predictions to real data one must relate the number of attempted improvements to something measurable. It is not straightforward to measure the effort that has gone into improving a technology, and to compare to real data one must use proxies. The most commonly used proxy is cumulative production, but other possibilities include cumulative investment, installed capacity, R&D expenditure, or even time. The best proxy for innovation effort is a subject of serious debate in the literature [15, 16, 11, 26, 22].

Possible Extensions to the Model

There are a variety of possible ways to extend the model to make it more realistic. For example, the model currently assumes that the design network described by the DSM is constant through time, but often improvements to a technology come about by modifying the design network. One can po-

³One problem that must be considered is that of resolution. As an approximation a DSM can be constructed the coarse level of entire systems, e.g. "electrical system", "fuel system", or it can be constructed more accurately at the microscopic level in terms of individual parts. In general these will give different design complexities.

tentially extend the model by adding an evolutionary model for the generation of new DSMs.

The possibility that the design complexity d^* changes through time suggests another empirical prediction. According to our theory, when d^* changes, α changes as well. One can conceivably examine an historical sequence of design matrices, compute their values of d^* , and compare the predicted $\alpha \sim 1/d^*$ to the corresponding observed values of α in the corresponding periods in time. Our theory predicts that these should be positively correlated.

We have assumed a particular model of learning in which improvement attempts are made at random, with no regard to the history of previous improvements or knowledge of the technology. An intelligent designer should be able to do better, drawing on his or her knowledge of science, engineering, and present and past designs. While an accurate model of such a complex process is likely to be difficult, it is possible to alter the model here so that innovation attempts are relative to the current design, rather than independent of it. This could potentially alter the predictions of the model.

Discussion

We have developed a simplified version of the model of Auerwald et al. [4], which predicts the improvement of cost as a function of the number of innovation attempts. While we have formulated the model in terms of cost, one could equally well have used any performance measure of the technology that has the property of being additive across the components. Our analysis makes clear predictions about the trajectories of technology improvement. The mean behavior of the cost is described by a power law with exponent $\alpha = 1/(d^*\gamma)$, where d^* is the design complexity, and γ describes the intrinsic difficulty of improving individual components. In the case of constant connectivity (out-degree) the design complexity is just

the connectivity, but in general it can depend on details of the design matrix, as spelled out in Eq. [7]. In addition, the range of variation in technological improvement trajectories depends on the number of critical bottlenecks. This number coincides with the total number of components n in the case of constant connectivity, but in general the number of worst bottlenecks is less than this, and depends on the detailed arrangement of the interactions in the design.

Many studies in the past have discussed effects that contribute to technological improvement, such as learning-by-doing, R&D, or capital investment. Our approach here is generic in the sense that it could apply to any of these. As long as these mechanisms cause innovation attempts that can be modeled as a process of trial and error, any of them can potentially be described by the model we have developed here.

Our analysis makes a new contribution by connecting the literature on the historical analysis of performance curves to that on the engineering design properties of a technology. We make a prediction about how the features of a design influence its rate of improvement, focusing attention on the interactions of components as codified in the design structure matrix. Perhaps most importantly, we pose several falsifiable propositions. Our analysis illustrates how the same evolutionary process can display either historical contingency or steady change, depending on the design. Our theory suggests that it may be possible to influence the long-term rate of improvement of a technology by reducing the connectivity between the components. Such an understanding of how the design features of a technology affect its evolution will aid engineering design, as well as science and technology policy.

ACKNOWLEDGMENTS. JM, DF, and JT gratefully acknowledge financial support from NSF Grant SBE0738187 and SR similarly acknowledges support from NSF Grant DMR0535503. We thank Yonathan Schwarzkopf, and Aaron Clauset for helpful conversations and suggestions. We thank Sidharth Rupani and Daniel Whitney for useful correspondence.

- Stephan Alberth. Forecasting technology costs via the experience curve – myth or magic? *Technological Forecasting and Social Change*, 75(7):952–983, September 2008.
- L. Argote and D. Eppl. Learning curves in manufacturing. *Science*, 247(4945):920–924, 1990.
- K. J. Arrow. The economic implications of learning by doing. *Review of Economic Studies*, 29:155–73, 1962.
- P. Auerwald, S. Kauffman, J. Lobo, and K. Shell. The production recipes approach to modeling technological innovation: An application to learning by doing. *Journal of Economic Dynamics & Control*, 24(3):389–450, 2000.
- C. Y. Baldwin and K. B. Clark. *Design Rules*. Cambridge, Mass.: MIT Press, 2000.
- W. N. Bryan and N. Harter. Studies in the telegraphic language: The acquisition of a hierarchy of habits. *Psychological Review*, 6:345–375, 1899.
- S. Chen and E. Huang. A systematic approach for supply chain improvement using design structure matrix. *Journal of Intelligent Manufacturing*, 18(2):285–299, Apr 2007.
- J. Judson D. E. Whitney, Q. Dong and G. Mascoli. Introducing knowledge-based engineering into an interconnected product development process. *Proceedings of the 1999 ASME Design Engineering Technical Conferences*, 1999.
- J. M. Dutton and A. Thomas. Treating progress functions as a managerial opportunity. *The Academy of Management Review*, 9(2):235–247, 1984.
- H. Ebbinghaus. *Memory: A Contribution to Experimental Psychology*. New York: Columbia University, 1885.
- C. Goddard. Debunking the learning curve. *IEEE Transactions on Components, Hybrids, and Manufacturing Technology*, 5(4):328–335, 1982.
- Boston Consulting Group. *Perspectives on Experience*. Boston, MA, 1972.
- B. A. Huberman. The dynamics of organizational learning. *Comput. Math. Organ. Theory*, 7(2):145–201, 2001.
- J. E. Trancik J. McNerney, J. D. Farmer. Coal-electricity: Historical costs and cost modeling. (in progress).
- H. Koh and C. L. Magee. A functional approach for studying technological progress: Application to information technology. *Technological Forecasting and Social Change*, 73(9):1061–1083, Nov 2006.
- H. Koh and C. L. Magee. A functional approach for studying technological progress: Extension to energy technology. *Technological Forecasting and Social Change*, 75(6):735–758, Jul 2008.
- P. D. Maycock. The world photovoltaic market. Technical report, PV Energy Systems, January 2002.
- A. McDonald and L. Schratzenholzer. Learning rates for energy technologies. *Energy Policy*, 29(4):255–261, 2001.
- G. E. Moore. Craming more components onto integrated circuits. *Electronics Magazine*, 38, 1965.
- J. F. Muth. Search theory and the manufacturing progress function. *Management Science*, 32(8):948–962, 1986.
- G. F. Nemet. Beyond the learning curve: factors influencing cost reductions in photovoltaics. *Energy Policy*, 34:3218–3232, 2006.
- William D. Nordhaus. The perils of the learning model for modeling endogenous technological change. SSRN eLibrary, 2009.
- P. F. Ostwald and J. B. Reisdorf. Measurement of technology progress and capital cost for nuclear, coal-fired, and gas-fired power plants using the learning curve. *Engineering and Process Economics*, 4(4):435–454, 1979.
- J. W. Rivkin and N. Siggelkow. Patterned interactions in complex systems: Implications for exploration. *Management Science*, 53(7):1068–1085, 2007.
- R. P. Smith S. D. Eppinger, D. E. Whitney and D. A. Gebala. A model-based method for organizing tasks in product development. *Research in Engineering Design-Theory Applications and Concurrent engineering*, 6(1):1–13, 1994.
- G. Sinclair, S. Klepper, and W. Cohen. What's Experience Got to Do With It? Sources of Cost Reduction in a Large Specialty Chemicals Producer. *Management Science*, 46(1):28–45, 2000.
- D. V. Steward. The design structure-system—a method for managing the design of complex-systems. *IEEE Transactions on Engineering Management*, 28(3):71–74, 1981.
- Strategies-Unlimited. Photovoltaic five-year market forecast, 2002-2007. Technical Report PM-52, Strategies-Unlimited, March 2003.
- P. Thompson. *Handbook of Economics of Technical Change*, chapter Learning by Doing. Elsevier/North-Holland, 2009.
- C. Wene. *Experience Curves for Energy Technology Policy*. International Energy Agency, Paris, 2000.
- T. P. Wright. Factors affecting the cost of airplanes. *Journal of Aeronautical Science*, 3(4):122–128, 1936.